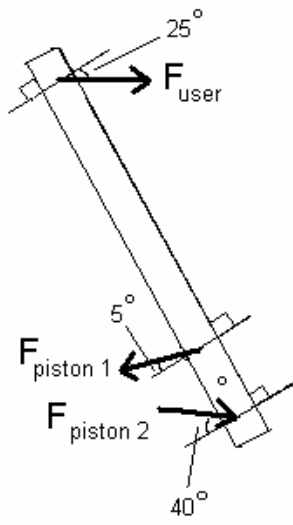


Appendix J



(positive clockwise):

$$\Sigma M_p = F_{user}(\cos 25^\circ)(2.92) - F_{piston1}(\cos 5^\circ)(.333) - F_{piston2}(\cos 40^\circ)(.417) = 0$$

$F_{user \text{ min}}$: F_{user} will be minimum when each of the pistons is set on the lowest setting, 5 lbs.

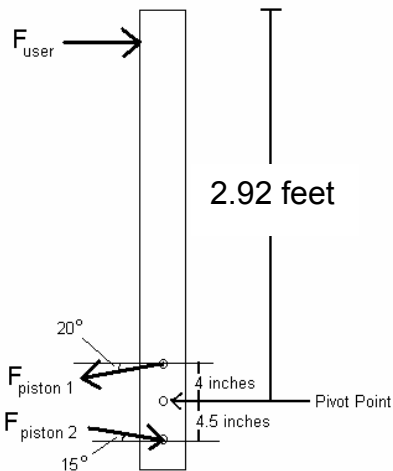
$$F_{user \text{ min}}(\cos 25^\circ)(2.92 \text{ ft}) - (5 \text{ lb})(\cos 5^\circ)(.417 \text{ ft}) - (5 \text{ lb})(\cos 40^\circ)(.333 \text{ ft}) = 0$$

$$F_{user \text{ min}} = 3.70 \text{ lbs}$$

$F_{user \text{ max}}$: F_{user} will be maximum when $F_{piston1}$ is set on the maximum setting, 200 lbs ($F_{piston2}$ is being shortened and can therefore only produce 5 lbs force).

$$F_{user \text{ max}}(\cos 25^\circ)(2.92 \text{ ft}) - (200 \text{ lb})(\cos 5^\circ)(.417 \text{ ft}) - (5 \text{ lb})(\cos 40^\circ)(.333 \text{ ft}) = 0$$

$$F_{user \text{ max}} = 93.08 \text{ lb}$$



(positive clockwise):

$$\Sigma M_p = F_{user}(2.92 \text{ ft}) - F_{piston1}(\cos 18.4^\circ)(.333 \text{ ft}) - F_{piston2}(\cos 15^\circ)(.417 \text{ ft}) = 0$$

$F_{user \text{ min}}$: F_{user} will be minimum when each of the pistons is set on the lowest setting, 5 lbs.

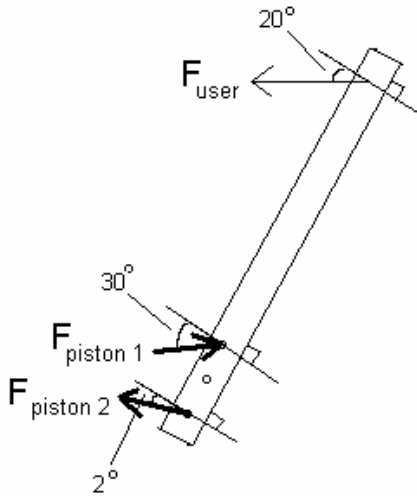
$$F_{user \text{ min}}(2.92 \text{ ft}) - (5 \text{ lb})(\cos 18.4^\circ)(.417 \text{ ft}) - (5 \text{ lb})(\cos 15^\circ)(.333 \text{ ft}) = 0$$

$$F_{user \text{ min}} = 3.59 \text{ lbs}$$

$F_{user \text{ max}}$: F_{user} will be maximum when $F_{piston1}$ is set on the maximum setting, 200 lbs ($F_{piston2}$ is being shortened and can therefore only produce 5 lbs force).

$$F_{user \text{ max}}(\cos 25^\circ)(2.92 \text{ ft}) - (200 \text{ lb})(\cos 18.4^\circ)(.417 \text{ ft}) - (5 \text{ lb})(\cos 15^\circ)(.333 \text{ ft}) = 0$$

$$F_{user \text{ max}} = 80.74 \text{ lb}$$



(positive clockwise):

$$\Sigma M_p = F_{user}(\cos 20^\circ)(2.92\text{ ft}) - F_{piston1}(\cos 30^\circ)(.333\text{ ft}) - F_{piston2}(\cos 2^\circ)(.417\text{ ft}) = 0$$

$F_{user\ min}$: F_{user} will be minimum when each of the pistons is set on the lowest setting, 5 lbs.

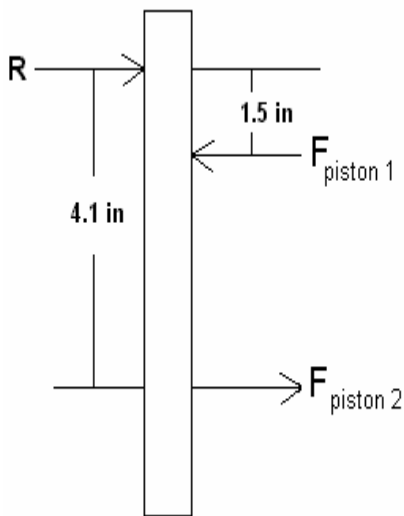
$$F_{user\ min}(2.92\text{ ft}) - (5\text{ lb})(\cos 30^\circ)(.417\text{ ft}) - (5\text{ lb})(\cos 2^\circ)(.333\text{ ft}) = 0$$

$$F_{user\ min} = 3.68\text{ lbs}$$

$F_{user\ max}$: F_{user} will be maximum when $F_{piston2}$ is set on the maximum setting, 200 lbs ($F_{piston1}$ is being shortened and can therefore only produce 5 lbs force).

$$F_{user\ max}(\cos 25^\circ)(2.92\text{ ft}) - (200\text{ lb})(\cos 30^\circ)(.417\text{ ft}) - (5\text{ lb})(\cos 2^\circ)(.333\text{ ft}) = 0$$

$$F_{user\ max} = 72.75\text{ lb}$$



(positive clockwise):

$F_{piston1}$ is at an angle of 5° above the horizontal and $F_{piston2}$ is at an angle of 22° below the horizontal.

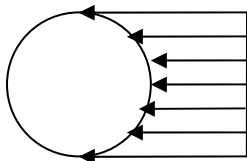
$$\Sigma M_R = F_{piston1}(1.5\text{ in})(\cos 5^\circ) - F_{piston2}(4.1\text{ in})(\cos 22^\circ)$$

The maximum torque will on the bolt will occur when $F_{piston2}$ is set to the maximum resistance ($F_{piston1}$ is being shortened and can therefore only produce 5 lbs force).

$$\Sigma M_R = (5\text{ lb})(1.5\text{ in})(\cos 5^\circ) - (200\text{ lb})(4.1\text{ in})(\cos 22^\circ) = 62.75\text{ lb}\cdot\text{inch}$$

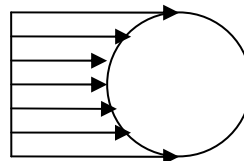
Since there is a larger component of force in the horizontal direction than in the vertical direction, the torque exerted in the vertical direction must be less than 62.75 lb and therefore does not need to be calculated.

Shear on bolt:



$$V = 500\text{ lbs}$$

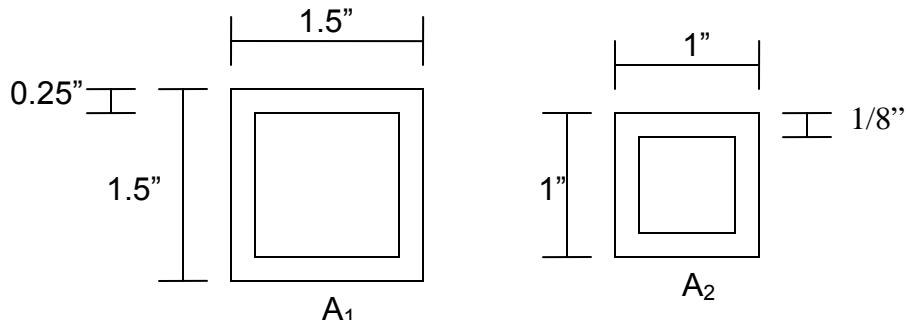
$\frac{1}{2}$ " Diameter
Grade 5 bolts



$$V = 500\text{ lbs}$$

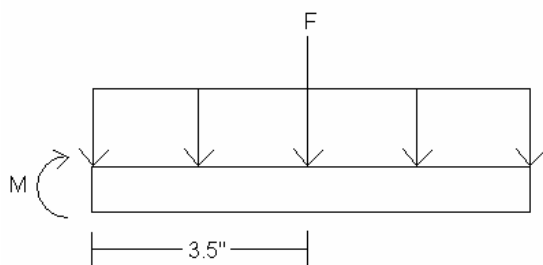
$$\tau = V/A = (500\text{ lb}/2)/(\pi(1/4)^2) = 2546\text{ psi}/2 = 1273\text{ psi}$$

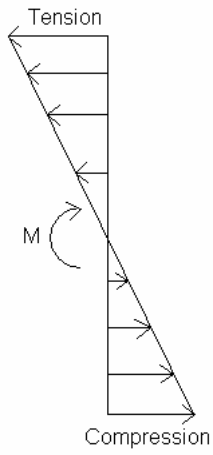
$T_{\text{critical}} = 75,000 \text{ psi}$ (from Rockcrawler.com)
 $1.3 \text{ ksi} \ll 75 \text{ ksi}$ so the design is safe.



$$A_1 = 1.5^2 - 1^2 = 1.25 \text{ in}^2$$
$$A_2 = 1^2 - 0.75^2 = 0.4375 \text{ in}^2$$

Bending on Cantilever Seat Mount

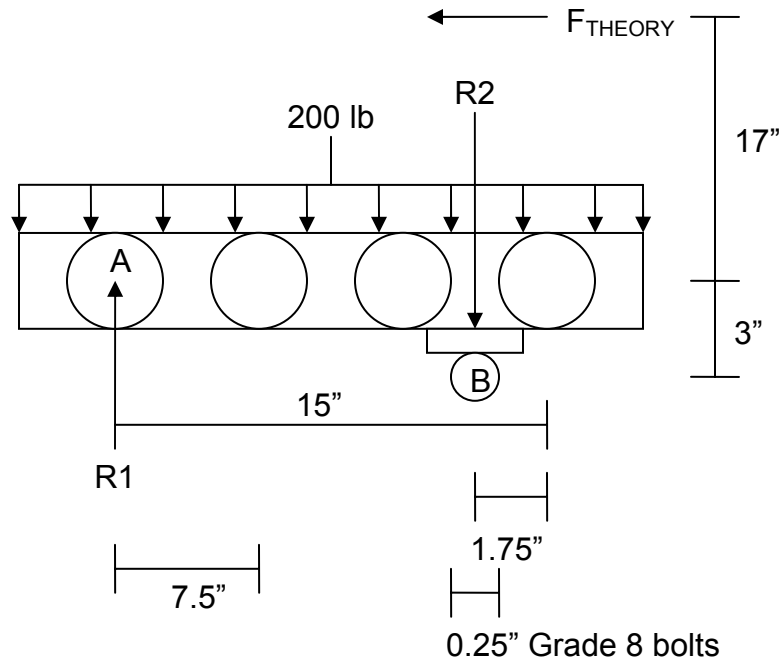




$$F = (400 \text{ lb}/18 \text{ in}) \cdot (7 \text{ in}) = 155.6 \text{ lb}$$
$$M = FD = (155.6 \text{ lb})(3.5 \text{ in}) = 544.4 \text{ in}\cdot\text{lb}$$

$$\tau_{\max}(1'') = M = 544.6 \text{ lb}\cdot\text{in} \ll T_{\text{critical}}; \text{ on the order ksi}$$

Seat Wheels



Shear on upper wheels normally:

$$T_{\text{critical}} = 91 \text{ ksi (Rockcrawler.com)}$$

$$T_{\text{simple}} = (V/4)/A = (200 \text{ lb}/4)/(\pi*(1/8)^2) = 1.02 \text{ ksi} \ll 91 \text{ ksi; safe}$$

Shear on lower wheels for R_{Theory} :

$$T_{\text{critical}} = 91 \text{ ksi} = V_{\text{critical}}/A = V_{\text{critical}}/(\pi(1/8)^2) \quad V_{\text{critical}} = 4467 \text{ lb}$$

For M about A:

$$M_A = -F_{\text{Theory}}(17'') + R_2(13.125'') = 0$$

$$R_2(13.125'') = F_{\text{Theory}}(17'')$$

For $R_2 = V_{\text{critical}}$:

$$F_{\text{Theory}} = 3449 \text{ lbs, so a user would need to exert this force at B for failure to occur.}$$

This is highly unlikely to happen due to the large force requirement.

For M about B:

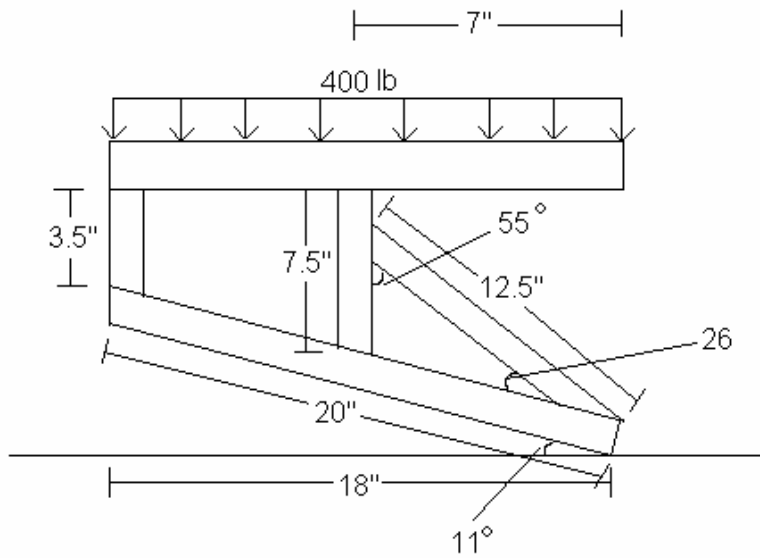
$$M_B = R_1(13.125'') - F_{\text{Theory}}(20'') = 0$$

$$R_1(13.125'') = F_{\text{Theory}}(20'')$$

For $R_1 = V_{\text{critical}}$:

$$F_{\text{Theory}} = 2931 \text{ lbs, so a user would need to exert this force at A for failure to occur, which is unlikely again due to the large force requirement.}$$

Seat Frame



Shear across vertical pillar bases:

$$A \text{ at } 0^\circ = 1.25 \text{ in}^2$$

$$A \text{ at } 11^\circ = 1.25 / (\cos 11^\circ) = 1.27 \text{ in}^2 \quad \text{weakest point is at } 11^\circ$$

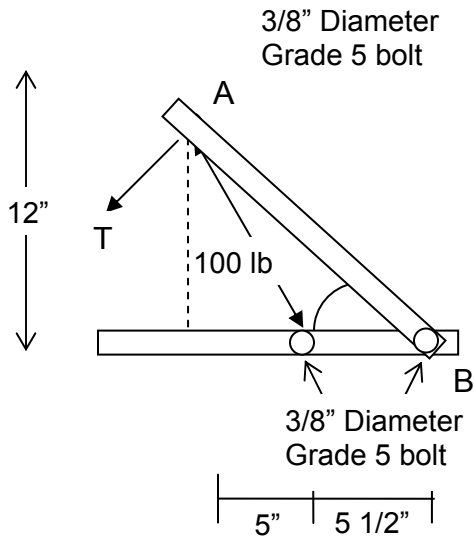
$$A \text{ at } 26^\circ = 1.25 / (\cos 26^\circ) = 1.39 \text{ in}^2$$

$$\tau = V/A = (400 \text{ lb}) / (1.27 \text{ in}^2) = 315 \text{ psi} \ll \tau_{\text{critical}}; \text{ on the order of ksi}$$

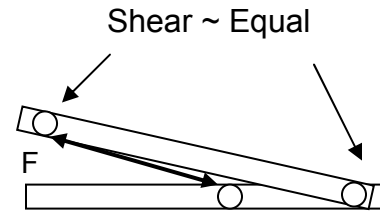
Buckling of vertical pillars:

This is not an issue because of the short columns, high moment of inertia, high elastic modulus, and low load. The buckling moments and shear will be far less than critical values.

Seat Assist



Shear on rod when down and tension when up



$$F = 100 \text{ lb} + \text{Spring Force}$$

As $\theta \rightarrow 0$

$$F = 100 \text{ lb} + (55.5 \text{ lb/in}) * (0.5 \text{ in})$$

$$F = 127.8 \text{ lbs}$$

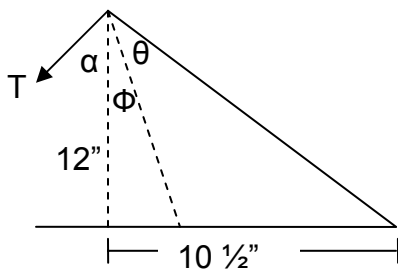
Thus, $F \ll V_{\text{crit}}$

$$\tau_{\text{crit}} = 75 \text{ ksi} = V_{\text{crit}} / A$$

$$= V_{\text{crit}} / \pi * (3/16")^2$$

$$V_{\text{crit}} = 8283 \text{ lbs}$$

$$\left. \begin{array}{l} V_A = 100 \text{ lbs} \\ V_B = 100 \text{ lbs} \end{array} \right\} \begin{array}{l} \text{Constant force} \\ \text{with respect to} \\ \text{piston. Both } V_A \\ \text{and } V_B \text{ much less} \\ \text{than } V_{\text{crit}} \end{array}$$



$$\Theta = 41.2^\circ$$

$$\Phi = 22.6^\circ$$

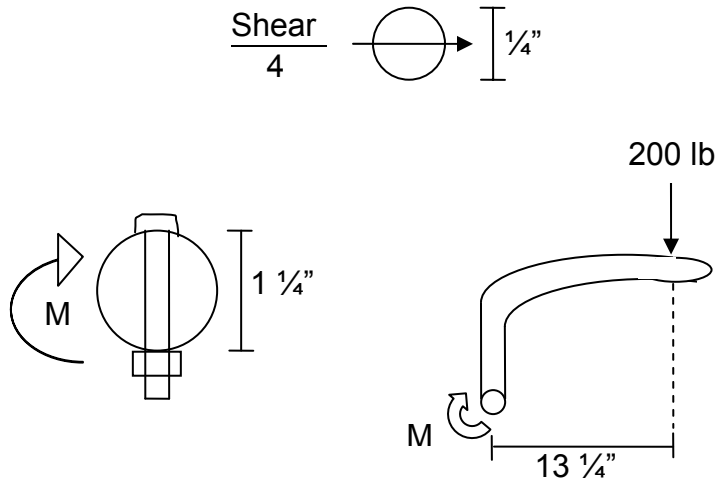
$$\alpha = 48.2^\circ$$

$$100 * \cos(22.6^\circ) = T * \cos(48.2^\circ)$$

$$T = 138.5 \text{ lbs}$$

EKG Handles

Across 4 bolt cross-sections



$$\tau_{\text{Crit}} = 75 \text{ ksi}$$

$$M = 200 \text{ lb} \cdot 13 \frac{1}{4} \text{\"} = 2650 \text{ lb}\cdot\text{in}$$

$$M = V \cdot 1 \frac{1}{4} \text{\"}$$

$$V = 2120 \text{ lbs} / 4 = 530 \text{ lbs}$$

$$\begin{aligned} \tau &= V/A = 530 \text{ lbs} / \pi \cdot (1/8 \text{\"})^2 \\ &= 10.8 \text{ ksi} \end{aligned}$$

$$10.8 \text{ ksi} < 75 \text{ ksi} \rightarrow \text{Safe}$$